

Exercise – 8.1

Question 1:

In $\triangle ABC$ right angled at B, AB = 24 cm, BC = 7 m. Determine

c

(i) sin A, cos A

(ii) sin C, cos C

Applying Pythagoras theorem for $\triangle ABC$, we obtain

$$AC^2 = AB^2 + BC^2$$

$$= (24 \text{ cm})^2 + (7 \text{ cm})^2$$

$$=(576+49)$$
 cm²

 $= 625 \text{ cm}^2$

$$\therefore AC = \sqrt{625} \text{ cm} = 25 \text{ cm}$$



(i)
$$\sin A = \frac{\text{Side opposite to } \angle A}{\text{Hypotenuse}} = \frac{\text{BC}}{\text{AC}}$$

$$=\frac{7}{25}$$

$$\cos A = \frac{\text{Side adjacent to } \angle A}{\text{Hypotenuse}} = \frac{AB}{AC} = \frac{24}{25}$$
(ii)



In the given figure find $\tan P - \cot R$



Applying Pythagoras theorem for Δ PQR, we obtain

 $PR^2 = PQ^2 + QR^2$

 $(13 \text{ cm})^2 = (12 \text{ cm})^2 + QR^2$

 $169 \text{ cm}^2 = 144 \text{ cm}^2 + QR^2$



 $25 \text{ cm}^2 = QR^2$

QR = 5 cm



$$= \frac{5}{12}$$

$$\cot R = \frac{\text{Side adjacent to } \angle R}{\text{Side opposite to } \angle R} = \frac{\text{QR}}{\text{PQ}}$$

$$= \frac{5}{12}$$

$$\tan P - \cot R = \frac{5}{12} - \frac{5}{12} = 0$$

Question 3:

If $\sin A = \frac{3}{4}$, calculate $\cos A$ and $\tan A$.

Let $\triangle ABC$ be a right-angled triangle, right-angled at point B.



Given that,



 $\sin A = \frac{3}{4}$ $\frac{BC}{AC} = \frac{3}{4}$

Let BC be 3k. Therefore, AC will be 4k, where k is a positive integer.

Applying Pythagoras theorem in $\triangle ABC$, we obtain

 $AC^{2} = AB^{2} + BC^{2}$ $(4k)^{2} = AB^{2} + (3k)^{2}$ $16k^{2} - 9k^{2} = AB^{2}$ $7k^{2} = AB^{2}$ $AB = \sqrt{7}k$ $\cos A = \frac{\text{Side adjacent to } \angle A}{\text{Hypotenuse}}$ $= \frac{AB}{AC} = \frac{\sqrt{7k}}{4k} = \frac{\sqrt{7}}{4}$ $\tan A = \frac{\text{Side opposite to } \angle A}{\text{Side adjacent to } \angle A}$ $= \frac{BC}{AB} = \frac{3k}{\sqrt{7k}} = \frac{3}{\sqrt{7}}$

Question 4:

Given 15 $\cot A = 8$. Find sin A and sec A

Consider a right-angled triangle, right-angled at B.



 $\cot A = \frac{1}{15}$ $\frac{AB}{BC} = \frac{8}{15}$

Let AB be 8*k*.Therefore, BC will be 15*k*, where *k* is a positive integer.

Applying Pythagoras theorem in $\triangle ABC$, we obtain

 $AC^{2} = AB^{2} + BC^{2}$ $= (8k)^{2} + (15k)^{2}$ $= 64k^{2} + 225k^{2}$ $= 289k^{2}$

AC = 17k



Question 5:

Given sec $\theta = \frac{13}{12}$, calculate all other trigonometric ratios.

Consider a right-angle triangle $\triangle ABC$, right-angled at point B.



If AC is 13k, AB will be 12k, where k is a positive integer.

Applying Pythagoras theorem in $\triangle ABC$, we obtain

$$(AC)^2 = (AB)^2 + (BC)^2$$

$$(13k)^2 = (12k)^2 + (BC)^2$$

 $169k^2 = 144k^2 + BC^2$

$$25k^2 = BC^2$$

BC = 5k



Question 6:

If $\angle A$ and $\angle B$ are acute angles such that $\cos A = \cos B$, then show that

 $\angle A = \angle B.$

Let us consider a triangle ABC in which $CD \perp AB$.



It is given that

 $\cos A = \cos B$

$$\Rightarrow \frac{AD}{AC} = \frac{BD}{BC} \dots (1)$$

We have to prove $\angle A = \angle B$. To prove this, let us extend AC to P such that BC = CP.



From equation (1), we obtain

$\frac{AD}{BD} = \frac{AC}{BC}$		
$\Rightarrow \frac{AD}{BD} = \frac{AC}{CP}$	(By construction, we have $BC = CP$)	(2)

By using the converse of B.P.T,

CD||BP

 $\Rightarrow \angle ACD = \angle CPB$ (Corresponding angles) ... (3)

And, $\angle BCD = \angle CBP$ (Alternate interior angles) ... (4)

By construction, we have BC = CP.

 $\therefore \angle CBP = \angle CPB$ (Angle opposite to equal sides of a triangle) ... (5)

From equations (3), (4), and (5), we obtain

 $\angle ACD = \angle BCD \dots (6)$

In \triangle CAD and \triangle CBD,

 $\angle ACD = \angle BCD$ [Using equation (6)]

 \angle CDA = \angle CDB [Both 90°]

Therefore, the remaining angles should be equal.



 $\therefore \angle CAD = \angle CBD$

$$\Rightarrow \angle A = \angle B$$

Alternatively,

Let us consider a triangle ABC in which $CD \perp AB$.



It is given that,

 $\cos A = \cos B$ $\Rightarrow \frac{AD}{AC} = \frac{BD}{BC}$ $\Rightarrow \frac{AD}{BD} = \frac{AC}{BC}$ $Let \frac{AD}{BD} = \frac{AC}{BC} = k$

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\Rightarrow AD = k BD ... (1)
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And, $AC = k BC \dots (2)$

Using Pythagoras theorem for triangles CAD and CBD, we obtain

 $CD^2 = AC^2 - AD^2 \dots (3)$

And,
$$CD^2 = BC^2 - BD^2 \dots (4)$$

From equations (3) and (4), we obtain

 $AC^2 - AD^2 = BC^2 - BD^2$

 $\Rightarrow (k \text{ BC})^2 - (k \text{ BD})^2 = \text{BC}^2 - \text{BD}^2$



 $\Rightarrow k^2 (BC^2 - BD^2) = BC^2 - BD^2$

$$\Rightarrow k^2 = 1$$

$$\Rightarrow k = 1$$

Putting this value in equation (2), we obtain

AC = BC

 $\Rightarrow \angle A = \angle B$ (Angles opposite to equal sides of a triangle)

Question 7:

If
$$\cot \theta = \frac{7}{8}$$
, evaluate

(i) $\frac{(1+\sin\theta)(1-\sin\theta)}{(1+\cos\theta)(1-\cos\theta)}$ (ii) $\cot^2\theta$

Let us consider a right triangle ABC, right-angled at point B.



If BC is 7*k*, then AB will be 8*k*, where *k* is a positive integer.

Applying Pythagoras theorem in $\triangle ABC$, we obtain

 $AC^2 = AB^2 + BC^2$



 $=(8k)^{2}+(7k)^{2}$ $= 64k^2 + 49k^2$ $= 113k^{2}$ $AC = \sqrt{113}k$ $\sin \theta = \frac{\text{Side opposite to } \angle \theta}{\text{Hypotenuse}} = \frac{\text{AB}}{\text{AC}}$ $=\frac{8k}{\sqrt{113}k}=\frac{8}{\sqrt{113}}$ $\cos \theta = \frac{\text{Side adjacent to } \angle \theta}{\text{Hypotenuse}} = \frac{\text{BC}}{\text{AC}}$ $=\frac{7k}{\sqrt{113}k}=\frac{7}{\sqrt{113}}$ (i) $\frac{(1+\sin\theta)(1-\sin\theta)}{(1+\cos\theta)(1-\cos\theta)} = \frac{(1-\sin^2\theta)}{(1-\cos^2\theta)}$ $=\frac{1-\left(\frac{8}{\sqrt{113}}\right)^2}{1-\left(\frac{7}{\sqrt{113}}\right)^2}=\frac{1-\frac{64}{113}}{1-\frac{49}{113}}$ $=\frac{\frac{49}{113}}{\frac{64}{64}}=\frac{49}{64}$ 113

(ii)
$$\cot^2 \theta = (\cot \theta)^2 = \left(\frac{7}{8}\right)^2 = \frac{49}{64}$$

Question 8:

If 3 cot A

= 4. Check whether
$$\frac{1-\tan^2 A}{1+\tan^2 A} = \cos^2 A - \sin^2 A$$
 or not.

It is given that $3\cot A = 4$



Or, $\cot A = \overline{3}$

Consider a right triangle ABC, right-angled at point B.



If AB is 4k, then BC will be 3k, where k is a positive integer.

In $\triangle ABC$,

$$(AC)^2 = (AB)^2 + (BC)^2$$

 $=(4k)^{2}+(3k)^{2}$

 $= 16k^2 + 9k^2$

 $= 25k^{2}$

AC = 5k

EDUCATION CENTRE Where You Get Complete Knowledge $\cos A = \frac{\text{Side adjacent to } \angle A}{\text{Hypotenuse}} = \frac{\text{AB}}{\text{AC}}$ $=\frac{4k}{5k}=\frac{4}{5}$ $\sin A = \frac{\text{Side opposite to } \angle A}{\text{Hypotenuse}} = \frac{\text{BC}}{\text{AC}}$ $=\frac{3k}{5k}=\frac{3}{5}$ $\tan A = \frac{\text{Side opposite to } \angle A}{\text{Hypotenuse}} = \frac{\text{BC}}{\text{AB}}$ $=\frac{3k}{4k}=\frac{3}{4}$ $\frac{1-\tan^2 A}{1+\tan^2 A} = \frac{1-\left(\frac{3}{4}\right)^2}{1+\left(\frac{3}{4}\right)^2} = \frac{1-\frac{9}{16}}{1+\frac{9}{16}}$ $=\frac{\frac{7}{16}}{\frac{25}{25}}=\frac{7}{25}$ $\cos^2 A - \sin^2 A = \left(\frac{4}{5}\right)^2 - \left(\frac{3}{5}\right)^2$

$$= \frac{16}{25} - \frac{9}{25} = \frac{7}{25}$$

$$\therefore \frac{1 - \tan^2 A}{1 + \tan^2 A} = \cos^2 A - \sin^2 A$$

Question 9:

In $\triangle ABC$, right angled at B. If $\tan A = \frac{1}{\sqrt{3}}$, find the value of

- (i) $\sin A \cos C + \cos A \sin C$
- (ii) $\cos A \cos C \sin A \sin C$



If BC is k, then AB will be $\sqrt{3}k$, where k is a positive integer.

In ΔABC,

 $AC^{2} = AB^{2} + BC^{2}$ $= (\sqrt{3}k)^{2} + (k)^{2}$ $= 3k^{2} + k^{2} = 4k^{2}$ $\therefore AC = 2k$ $\sin A = \frac{\text{Side opposite to } \angle A}{\text{Hypotenuse}} = \frac{BC}{AC} = \frac{k}{2k} = \frac{1}{2}$ $\cos A = \frac{\text{Side adjacent to } \angle A}{\text{Hypotenuse}} = \frac{AB}{AC} = \frac{\sqrt{3}k}{2k} = \frac{\sqrt{3}}{2}$ $\sin C = \frac{\text{Side opposite to } \angle C}{\text{Hypotenuse}} = \frac{AB}{AC} = \frac{\sqrt{3}k}{2k} = \frac{\sqrt{3}}{2}$ $\cos C = \frac{\text{Side adjacent to } \angle C}{\text{Hypotenuse}} = \frac{BC}{AC} = \frac{k}{2k} = \frac{1}{2}$ (i) sin A cos C + cos A sin C



$$=\frac{4}{4}=1$$

(ii) cos A cos C – sin A sin C

$$= \left(\frac{\sqrt{3}}{2}\right) \left(\frac{1}{2}\right) - \left(\frac{1}{2}\right) \left(\frac{\sqrt{3}}{2}\right) = \frac{\sqrt{3}}{4} - \frac{\sqrt{3}}{4} = 0$$

Question 10:

In \triangle PQR, right angled at Q, PR + QR = 25 cm and PQ = 5 cm. Determine the values of sin P, cos P and tan P.

Given that, PR + QR = 25

PQ = 5

Let PR be *x*.

Therefore, QR = 25 - x



Applying Pythagoras theorem in Δ PQR, we obtain

50*x*

$$PR^{2} = PQ^{2} + QR^{2}$$
$$x^{2} = (5)^{2} + (25 - x)^{2}$$
$$x^{2} = 25 + 625 + x^{2} - 50x = 650$$



x = 13

Therefore, PR = 13 cm

QR = (25 - 13) cm = 12 cm

 $\sin P = \frac{\text{Side opposite to } \angle P}{\text{Hypotenuse}} = \frac{\text{QR}}{\text{PR}} = \frac{12}{13}$ $\cos P = \frac{\text{Side adjacent to } \angle P}{\text{Hypotenuse}} = \frac{\text{PQ}}{\text{PR}} = \frac{5}{13}$ $\tan P = \frac{\text{Side opposite to } \angle P}{\text{Side adjacent to } \angle P} = \frac{\text{QR}}{\text{PQ}} = \frac{12}{5}$

Question 11:

State whether the following are true or false. Justify your answer.

(i) The value of tan A is always less than 1.

(ii) sec A = $\frac{12}{5}$ for some value of angle A.

(iii) cos A is the abbreviation used for the cosecant of angle A.

(iv) cot A is the product of cot and A

(v) $\sin \theta = \frac{4}{3}$, for some angle θ

(i) Consider a $\triangle ABC$, right-angled at B.





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 $\tan A = \frac{\text{Side opposite to } \angle A}{\text{Side adjacent to } \angle A}$ $= \frac{12}{5}$ But $\frac{12}{5} > 1$ $\therefore \tan A > 1$

So, $\tan A < 1$ is not always true.

Hence, the given statement is false.



Let AC be 12k, AB will be 5k, where k is a positive integer.

Applying Pythagoras theorem in $\triangle ABC$, we obtain

 $AC^{2} = AB^{2} + BC^{2}$ $(12k)^{2} = (5k)^{2} + BC^{2}$ $144k^{2} = 25k^{2} + BC^{2}$ $BC^{2} = 119k^{2}$



BC = 10.9k

It can be observed that for given two sides AC = 12k and AB = 5k,

BC should be such that,

AC - AB < BC < AC + AB

12k - 5k < BC < 12k + 5k

7k < BC < 17 k

However, BC = 10.9k. Clearly, such a triangle is possible and hence, such value of sec A is possible.

Hence, the given statement is true.

(iii) Abbreviation used for cosecant of angle A is cosec A. And cos A is the abbreviation used for cosine of angle A.

Hence, the given statement is false.

(iv) cot A is not the product of cot and A. It is the cotangent of $\angle A$.

Hence, the given statement is false.

(v)
$$\sin \theta = \frac{4}{3}$$

We know that in a right-angled triangle,

 $\sin \theta = \frac{\text{Side opposite to } \angle \theta}{\text{Hypotenuse}}$

In a right-angled triangle, hypotenuse is always greater than the remaining two sides. Therefore, such value of sin θ is not possible.

Hence, the given statement is false



Question 1:

(i) $\sin 60^{\circ} \cos 30^{\circ} + \sin 30^{\circ} \cos 60^{\circ}$

(ii)
$$2\tan^2 45^\circ + \cos^2 30^\circ - \sin^2 60^\circ$$

cos 45°

(iii) $\overline{\sec 30^\circ + \csc 30^\circ}$

$$\frac{\sin 30^\circ + \tan 45^\circ - \csc 60^\circ}{\cos 20^\circ + \cos 60^\circ + \cot 45^\circ}$$

(iv) $\sec 30^\circ + \cos 60^\circ + \cot 45^\circ$

(v)
$$\frac{5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$$

(i) $\sin 60^{\circ} \cos 30^{\circ} + \sin 30^{\circ} \cos 60^{\circ}$

$$= \left(\frac{\sqrt{3}}{2}\right) \left(\frac{\sqrt{3}}{2}\right) + \left(\frac{1}{2}\right) \left(\frac{1}{2}\right)$$
$$= \frac{3}{4} + \frac{1}{4} = \frac{4}{4} = 1$$

(ii) $2\tan^2 45^\circ + \cos^2 30^\circ - \sin^2 60^\circ$

$$= 2(1)^{2} + \left(\frac{\sqrt{3}}{2}\right)^{2} - \left(\frac{\sqrt{3}}{2}\right)^{2}$$
$$= 2 + \frac{3}{4} - \frac{3}{4} = 2$$

(iii)
$$\frac{\cos 45^{\circ}}{\sec 30^{\circ} + \csc 30^{\circ}}$$



Where You Get Complete Knowledge $= \frac{\frac{1}{\sqrt{2}}}{\frac{2}{\sqrt{3}} + 2} = \frac{\frac{1}{\sqrt{2}}}{\frac{2 + 2\sqrt{3}}{\sqrt{3}}}$ $= \frac{\sqrt{3}}{\sqrt{2}(2 + 2\sqrt{3})} = \frac{\sqrt{3}}{2\sqrt{2} + 2\sqrt{6}}$ $= \frac{\sqrt{3}(2\sqrt{6} - 2\sqrt{2})}{(2\sqrt{6} + 2\sqrt{2})(2\sqrt{6} - 2\sqrt{2})}$ $= \frac{2\sqrt{3}(\sqrt{6} - \sqrt{2})}{(2\sqrt{6})^{2} - (2\sqrt{2})^{2}} = \frac{2\sqrt{3}(\sqrt{6} - \sqrt{2})}{24 - 8} = \frac{2\sqrt{3}(\sqrt{6} - \sqrt{2})}{16}$ $= \frac{\sqrt{18} - \sqrt{6}}{8} = \frac{3\sqrt{2} - \sqrt{6}}{8}$ sin 30° + tan 45° - cosec60°

(iv) $\frac{\sin 30^\circ + \tan 43^\circ - \csc 60^\circ}{\sec 30^\circ + \cos 60^\circ + \cot 45^\circ}$

Question 2:

Choose the correct option and justify your choice.

 $\frac{2 \tan 30^{\circ}}{1 + \tan^2 30^{\circ}} =$ (A). sin60° (B). cos60° (C). tan60° (D). sin30° (ii) $\frac{1 - \tan^2 45^{\circ}}{1 + \tan^2 45^{\circ}} =$ (A). tan90° (B). 1



(C). sin45°

(D). 0

- (iii) sin2A = 2sinA is true when A =
- (A). 0°
- (B). 30°
- (C). 45°
- (D). 60°

(iv)
$$\frac{2\tan 30^{\circ}}{1-\tan^2 30^{\circ}} =$$

- (A). cos60°
- (B). sin60°
- (C). tan60°
- (D). sin30°

(i) $\frac{2 \tan 30^{\circ}}{1 + \tan^2 30^{\circ}}$

$$=\frac{2\left(\frac{1}{\sqrt{3}}\right)}{1+\left(\frac{1}{\sqrt{3}}\right)^2} = \frac{\frac{2}{\sqrt{3}}}{1+\frac{1}{3}} = \frac{\frac{2}{\sqrt{3}}}{\frac{4}{3}}$$
$$=\frac{\frac{6}{4\sqrt{3}}}{\frac{4}{3}} = \frac{\sqrt{3}}{2}$$

$$\sin 60^\circ = \frac{\sqrt{3}}{2}$$

Out of the given alternatives, only

Hence, (A) is correct.



(ii) $\frac{1 - \tan^2 45^\circ}{1 + \tan^2 45^\circ}$

$$=\frac{1-(1)^2}{1+(1)^2}=\frac{1-1}{1+1}=\frac{0}{2}=0$$

Hence, (D) is correct.

(iii)Out of the given alternatives, only $A = 0^{\circ}$ is correct.

As $\sin 2A = \sin 0^\circ = 0$

 $2 \sin A = 2\sin 0^\circ = 2(0) = 0$

Hence, (A) is correct.

(iv)
$$\frac{2 \tan 30^{\circ}}{1 - \tan^2 30^{\circ}}$$

= $\frac{2\left(\frac{1}{\sqrt{3}}\right)}{1 - \left(\frac{1}{\sqrt{3}}\right)^2} = \frac{\frac{2}{\sqrt{3}}}{1 - \frac{1}{3}} = \frac{\frac{2}{\sqrt{3}}}{\frac{2}{3}}$
= $\sqrt{3}$

Out of the given alternatives, only $\tan 60^\circ = \sqrt{3}$

Hence, (C) is correct.



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$$=\frac{\frac{1}{2}+1-\frac{2}{\sqrt{3}}}{\frac{2}{\sqrt{3}}+\frac{1}{2}+1}=\frac{\frac{3}{2}-\frac{2}{\sqrt{3}}}{\frac{3}{2}+\frac{2}{\sqrt{3}}}$$

$$=\frac{\frac{3\sqrt{3}-4}{2\sqrt{3}}}{\frac{3\sqrt{3}+4}{2\sqrt{3}}}=\frac{(3\sqrt{3}-4)}{(3\sqrt{3}+4)}$$

$$=\frac{(3\sqrt{3}-4)(3\sqrt{3}-4)}{(3\sqrt{3}+4)(3\sqrt{3}-4)}=\frac{(3\sqrt{3}-4)^2}{(3\sqrt{3})^2-(4)^2}$$

$$=\frac{27+16-24\sqrt{3}}{27-16}=\frac{43-24\sqrt{3}}{11}$$

(v)
$$\frac{5\cos^2 60^\circ + 4\sec^2 30^\circ - \tan^2 45^\circ}{\sin^2 30^\circ + \cos^2 30^\circ}$$

$$=\frac{5\left(\frac{1}{2}\right)^{2}+4\left(\frac{2}{\sqrt{3}}\right)^{2}-(1)^{2}}{\left(\frac{1}{2}\right)^{2}+\left(\frac{\sqrt{3}}{2}\right)^{2}}$$

$$=\frac{5\left(\frac{1}{4}\right) + \left(\frac{10}{3}\right) - 1}{\frac{1}{4} + \frac{3}{4}}$$
$$=\frac{\frac{15 + 64 - 12}{12}}{\frac{4}{4}} = \frac{67}{12}$$

Question 3:

If
$$\tan(A+B) = \sqrt{3}$$
 and $\tan(A-B) = \frac{1}{\sqrt{3}}$;



 $0^{\circ} < A + B \le 90^{\circ}$, A > B find A and B.

 $\tan (A + B) = \sqrt{3}$ $\Rightarrow \tan (A + B) = \tan 60$ $\Rightarrow A + B = 60 \dots (1)$ $\tan (A - B) = \frac{1}{\sqrt{3}}$ $\Rightarrow \tan (A - B) = \tan 30$ $\Rightarrow A - B = 30 \dots (2)$ On adding both equations, we obtain

$$2A = 90$$

$$\Rightarrow A = 45$$

From equation (1), we obtain

45 + B = 60

B = 15

Therefore, $\angle A = 45^{\circ}$ and $\angle B = 15^{\circ}$

Question 4:

State whether the following are true or false. Justify your answer.

(i) $\sin(A + B) = \sin A + \sin B$

- (ii) The value of $sin\theta$ increases as θ increases
- (iii) The value of $\cos \theta$ increases as θ increases
- (iv) $\sin\theta = \cos\theta$ for all values of θ



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(v) cot A is not defined for $A = 0^{\circ}$

(i) $\sin(A + B) = \sin A + \sin B$

Let $A = 30^{\circ}$ and $B = 60^{\circ}$

 $\sin (A + B) = \sin (30^{\circ} + 60^{\circ})$

 $= \sin 90^{\circ}$

= 1

 $\sin A + \sin B = \sin 30^\circ + \sin 60^\circ$

$$=\frac{1}{2}+\frac{\sqrt{3}}{2}=\frac{1+\sqrt{3}}{2}$$

Clearly, $\sin(A + B) \neq \sin A + \sin B$

Hence, the given statement is false.

(ii) The value of sin θ increases as θ increases in the interval of $0^{\circ} < \theta < 90^{\circ}$ as

 $\sin 0^\circ = 0$

$$\sin 30^{\circ} = \frac{1}{2} = 0.5$$
$$\sin 45^{\circ} = \frac{1}{\sqrt{2}} = 0.707$$
$$\sin 60^{\circ} = \frac{\sqrt{3}}{2} = 0.866$$

 $\sin 90^\circ = 1$

Hence, the given statement is true.

(iii) $\cos 0^\circ = 1$



It can be observed that the value of $\cos \theta$ does not increase in the interval of $0^{\circ} < \theta < 90^{\circ}$.

Hence, the given statement is false.

(iv) $\sin \theta = \cos \theta$ for all values of θ .

This is true when $\theta = 45^{\circ}$

As $\sin 45^\circ = \frac{1}{\sqrt{2}}$

 $\cos 45^\circ = \frac{1}{\sqrt{2}}$

It is not true for all other values of θ .

As
$$\sin 30^\circ = \frac{1}{2}$$
 and $\cos 30^\circ = \frac{\sqrt{3}}{2}$,

Hence, the given statement is false.

(v) cot A is not defined for $A = 0^{\circ}$

$$\cot A = \frac{\cos A}{\sin A},$$
$$\cot 0^{\circ} = \frac{\cos 0^{\circ}}{\sin 0^{\circ}} = \frac{1}{0} = \text{undefined}$$

Hence, the given statement is true.

Question 4:



State whether the following are true or false. Justify your answer.

(i)
$$\sin(A + B) = \sin A + \sin B$$

- (ii) The value of $\sin\theta$ increases as θ increases
- (iii) The value of $\cos \theta$ increases as θ increases
- (iv) $\sin\theta = \cos\theta$ for all values of θ
- (v) cot A is not defined for $A = 0^{\circ}$
- (i) $\sin(A + B) = \sin A + \sin B$

Let $A = 30^{\circ}$ and $B = 60^{\circ}$

 $\sin (A + B) = \sin (30^{\circ} + 60^{\circ})$

- $= \sin 90^{\circ}$
- = 1

 $\sin A + \sin B = \sin 30^\circ + \sin 60^\circ$

$$=\frac{1}{2}+\frac{\sqrt{3}}{2}=\frac{1+\sqrt{3}}{2}$$

Clearly, $sin (A + B) \neq sin A + sin B$

Hence, the given statement is false.

(ii) The value of sin θ increases as θ increases in the interval of $0^{\circ} < \theta < 90^{\circ}$ as

$$\sin 30^{\circ} = \frac{1}{2} = 0.5$$
$$\sin 45^{\circ} = \frac{1}{\sqrt{2}} = 0.707$$
$$\sin 60^{\circ} = \frac{\sqrt{3}}{2} = 0.866$$

 $\sin 0^\circ = 0$



 $\sin 90^\circ = 1$

Hence, the given statement is true.

(iii) $\cos 0^\circ = 1$ $\cos 30^\circ = \frac{\sqrt{3}}{2} = 0.866$ $\cos 45^\circ = \frac{1}{\sqrt{2}} = 0.707$ $\cos 60^\circ = \frac{1}{2} = 0.5$

 $\cos 90^\circ = 0$

It can be observed that the value of $\cos \theta$ does not increase in the interval of $0^{\circ} < \theta < 90^{\circ}$.

Hence, the given statement is false.

(iv) $\sin \theta = \cos \theta$ for all values of θ .

This is true when $\theta = 45^{\circ}$

 $\sin 45^\circ = \frac{1}{\sqrt{2}}$

 $\cos 45^\circ = \frac{1}{\sqrt{2}}$

It is not true for all other values of θ .

As
$$\sin 30^\circ = \frac{1}{2}$$
 and $\cos 30^\circ = \frac{\sqrt{3}}{2}$,

Hence, the given statement is false.

(v) $\cot A$ is not defined for $A = 0^{\circ}$

$$\operatorname{cot} A = \frac{\cos A}{\sin A},$$



 $\cot 0^\circ = \frac{\cos 0^\circ}{\sin 0^\circ} = \frac{1}{0}$ = undefined

Hence, the given statement is true.

Exercise – 8.3

Question 1:

Evaluate

(I) $\frac{\sin 18^{\circ}}{\cos 72^{\circ}}$

tan 26°

- (II) $\overline{\cot 64^{\circ}}$
- (III) $\cos 48^\circ \sin 42^\circ$
- (IV)cosec 31° sec 59°
- $\frac{\sin 18^{\circ}}{\cos 72^{\circ}} = \frac{\sin (90^{\circ} 72^{\circ})}{\cos 72^{\circ}}$ $= \frac{\cos 72^{\circ}}{\cos 72^{\circ}} = 1$ (II) $\frac{\tan 26^{\circ}}{\cot 64^{\circ}} = \frac{\tan (90^{\circ} 64^{\circ})}{\cot 64^{\circ}}$ $= \frac{\cot 64^{\circ}}{\cot 64^{\circ}} = 1$ (III) $\cos 48^{\circ} \sin 42^{\circ} = \cos (90^{\circ} 42^{\circ}) \sin 42^{\circ}$ $= \sin 42^{\circ} \sin 42^{\circ}$ = 0(IV) $\csc 31^{\circ} \sec 59^{\circ} = \csc (90^{\circ} 59^{\circ}) \sec 59^{\circ}$



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 $= \sec 59^\circ - \sec 59^\circ$

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= 0
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Question 2:

Show that

(I) $\tan 48^{\circ} \tan 23^{\circ} \tan 42^{\circ} \tan 67^{\circ} = 1$

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(II)\cos 38^\circ \cos 52^\circ - \sin 38^\circ \sin 52^\circ = 0
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(I) $\tan 48^{\circ} \tan 23^{\circ} \tan 42^{\circ} \tan 67^{\circ}$

 $= \tan (90^\circ - 42^\circ) \tan (90^\circ - 67^\circ) \tan 42^\circ \tan 67^\circ$

 $= \cot 42^{\circ} \cot 67^{\circ} \tan 42^{\circ} \tan 67^{\circ}$

 $= (\cot 42^{\circ} \tan 42^{\circ}) (\cot 67^{\circ} \tan 67^{\circ})$

=(1)(1)

= 1

(II) $\cos 38^\circ \cos 52^\circ - \sin 38^\circ \sin 52^\circ$

 $= \cos (90^{\circ} - 52^{\circ}) \cos (90^{\circ} - 38^{\circ}) - \sin 38^{\circ} \sin 52^{\circ}$

 $= \sin 52^\circ \sin 38^\circ - \sin 38^\circ \sin 52^\circ$

= 0

Question 3:

If $\tan 2A = \cot (A - 18^\circ)$, where 2A is an acute angle, find the value of A.

Given that,

 $\tan 2A = \cot (A - 18^\circ)$

 $\cot (90^{\circ} - 2A) = \cot (A - 18^{\circ})$



 $90^{\circ} - 2A = A - 18^{\circ}$

 $108^{\circ} = 3A$

$$A = 36^{\circ}$$

Question 4:

If tan A = cot B, prove that $A + B = 90^{\circ}$

Given that,

 $\tan A = \cot B$

 $\tan A = \tan (90^\circ - B)$

 $A = 90^{\circ} - B$

 $A + B = 90^{\circ}$

Question 5:

If sec $4A = cosec (A - 20^\circ)$, where 4A is an acute angle, find the value of A.

Given that,

sec $4A = cosec (A - 20^{\circ})$ cosec $(90^{\circ} - 4A) = cosec (A - 20^{\circ})$ $90^{\circ} - 4A = A - 20^{\circ}$ $110^{\circ} = 5A$ $A = 22^{\circ}$

Question 6:

If A, Band C are interior angles of a triangle ABC then show that

$$\sin\!\left(\frac{\mathrm{B}\!+\!\mathrm{C}}{2}\right)\!=\!\cos\!\frac{\mathrm{A}}{2}$$



Where You Get Complete Knowledge

We know that for a triangle ABC,

$$\angle A + \angle B + \angle C = 180^{\circ}$$

$$\angle B + \angle C = 180^{\circ} - \angle A$$
$$\frac{\angle B + \angle C}{2} = 90^{\circ} - \frac{\angle A}{2}$$
$$\sin\left(\frac{B + C}{2}\right) = \sin\left(90^{\circ} - \frac{A}{2}\right)$$
$$= \cos\left(\frac{A}{2}\right)$$

Question 7:

Express sin $67^{\circ} + \cos 75^{\circ}$ in terms of trigonometric ratios of angles between 0° and 45° .

$$\sin 67^{\circ} + \cos 75^{\circ}$$

= sin (90° - 23°) + cos (90° - 15°)
= cos 23° + sin 15°
Exercise - 8.4

Question 1:

Express the trigonometric ratios sin A, sec A and tan A in terms of cot A.

We know that,

$$\csc^{2}A = 1 + \cot^{2} A$$
$$\frac{1}{\csc^{2}A} = \frac{1}{1 + \cot^{2} A}$$
$$\sin^{2} A = \frac{1}{1 + \cot^{2} A}$$
$$\sin A = \pm \frac{1}{\sqrt{1 + \cot^{2} A}}$$

 $\sqrt{1 + \cot^2 A}$ will always be positive as we are adding two positive quantities.



Where You Get Complete Knowledge

Sin A = $\frac{1}{\sqrt{1 + \cot^2 A}}$

We know that, $\tan A = \frac{\sin A}{\cos A}$

However,
$$\cot A = \frac{\cos A}{\sin A}$$

Therefore,
$$\tan A = \frac{1}{\cot A}$$

Also,
$$\sec^2 A = 1 + \tan^2 A$$

$$= 1 + \frac{1}{\cot^2 A}$$
$$= \frac{\cot^2 A + 1}{\cot^2 A}$$

$$\sec A = \frac{\sqrt{\cot^2 A + 1}}{\cot A}$$

Question 2:

Write all the other trigonometric ratios of $\angle A$ in terms of sec A.

We know that,

$$\cos A = \frac{1}{\sec A}$$

Also, $\sin^2 A + \cos^2 A = 1$

$$\sin^2 A = 1 - \cos^2 A$$

$$\sin A = \sqrt{1 - \left(\frac{1}{\sec A}\right)^2}$$
$$= \sqrt{\frac{\sec^2 A - 1}{\sec^2 A}} = \frac{\sqrt{\sec^2 A - 1}}{\sec A}$$



$$\tan^{2}A + 1 = \sec^{2}A$$
$$\tan^{2}A = \sec^{2}A - 1$$
$$\tan A = \sqrt{\sec^{2}A - 1}$$
$$\cot A = \frac{\cos A}{\sin A} = \frac{\frac{1}{\sec A}}{\frac{\sqrt{\sec^{2}A - 1}}{\sec A}}$$
$$= \frac{1}{\sqrt{\sec^{2}A - 1}}$$
$$\csc A = \frac{1}{\sin A} = \frac{\sec A}{\sqrt{\sec^{2}A - 1}}$$

Evaluate

(i) $\frac{\sin^2 63^\circ + \sin^2 27^\circ}{\cos^2 17^\circ + \cos^2 73^\circ}$

(ii) $\sin 25^{\circ} \cos 65^{\circ} + \cos 25^{\circ} \sin 65^{\circ}$

(i)
$$\frac{\sin^2 63^\circ + \sin^2 27^\circ}{\cos^2 17^\circ + \cos^2 73^\circ}$$
$$= \frac{\left[\sin \left(90^\circ - 27^\circ\right)\right]^2 + \sin^2 27^\circ}{\left[\cos \left(90^\circ - 73^\circ\right)\right]^2 + \cos^2 73^\circ}$$
$$= \frac{\left[\cos 27^\circ\right]^2 + \sin^2 27^\circ}{\left[\sin 73^\circ\right]^2 + \cos^2 73^\circ}$$
$$= \frac{\cos^2 27^\circ + \sin^2 27^\circ}{\sin^2 73^\circ + \cos^2 73^\circ}$$
$$= \frac{1}{1} (As \sin^2 A + \cos^2 A = 1)$$
$$= 1$$



Where You Get Complete Knowledge

(ii) $\sin 25^{\circ} \cos 65^{\circ} + \cos 25^{\circ} \sin 65^{\circ}$

$$= (\sin 25^{\circ}) \{ \cos(90^{\circ} - 25^{\circ}) \} + \cos 25^{\circ} \{ \sin(90^{\circ} - 25^{\circ}) \}$$
$$= (\sin 25^{\circ}) (\sin 25^{\circ}) + (\cos 25^{\circ}) (\cos 25^{\circ})$$

 $=\sin^2 25^\circ + \cos^2 25^\circ$

 $= 1 (As \sin^2 A + \cos^2 A = 1)$

Question 4:

Choose the correct option. Justify your choice.

(i) $9 \sec^2 A - 9 \tan^2 A =$
(A) 1
(B) 9
(C) 8
(D) 0
(ii) $(1 + \tan \theta + \sec \theta) (1 + \cot \theta - \csc \theta)$
(A) 0
(B) 1
(C) 2
(D) -1
(iii) $(\sec A + \tan A) (1 - \sin A) =$
(A) secA
(B) sinA
(C) cosecA



(D) cosA

 $1 + \tan^2 A$

- (iv) $\overline{1 + \cot^2 A}$
- (A) $sec^2 A$

(B) –1

- (C) $\cot^2 A$
- (D) $tan^2 A$
- (i) $9 \sec^2 A 9 \tan^2 A$
- $=9\left(\sec^{2}A \tan^{2}A\right)$
- $= 9 (1) [As sec^{2} A tan^{2} A = 1]$

```
= 9
```

Hence, alternative (B) is correct.

Question 5:

Prove the following identities, where the angles involved are acute angles for which the expressions are defined.

$$s(i) (\csc \theta - \cot \theta)^{2} = \frac{1 - \cos \theta}{1 + \cos \theta}$$
L.H.S.= $(\csc \theta - \cot \theta)^{2}$

$$= \left(\frac{1}{\sin \theta} - \frac{\cos \theta}{\sin \theta}\right)^{2}$$

$$= \frac{(1 - \cos \theta)^{2}}{(\sin \theta)^{2}} = \frac{(1 - \cos \theta)^{2}}{\sin^{2} \theta}$$

$$= \frac{(1 - \cos \theta)^{2}}{1 - \cos^{2} \theta} = \frac{(1 - \cos \theta)^{2}}{(1 - \cos \theta)(1 + \cos \theta)} = \frac{1 - \cos \theta}{1 + \cos \theta}$$
=R.H.S.



$$\frac{\cos A}{1+\sin A} + \frac{1+\sin A}{\cos A} = 2 \sec A$$

$$L.H.S. = \frac{\cos A}{1+\sin A} + \frac{1+\sin A}{\cos A}$$

$$= \frac{\cos^2 A + (1+\sin A)^2}{(1+\sin A)(\cos A)}$$

$$= \frac{\cos^2 A + (1+\sin A)(\cos A)}{(1+\sin A)(\cos A)}$$

$$= \frac{\sin^2 A + \cos^2 A + 1 + 2\sin A}{(1+\sin A)(\cos A)}$$

$$= \frac{1+1+2\sin A}{(1+\sin A)(\cos A)} = \frac{2+2\sin A}{(1+\sin A)(\cos A)}$$

$$= \frac{2(1+\sin A)}{(1+\sin A)(\cos A)} = \frac{2}{\cos A} = 2 \sec A$$

$$= R.H.S.$$

(iii)
$$\frac{\tan\theta}{1-\cot\theta} + \frac{\cot\theta}{1-\tan\theta} = 1 + \sec\theta\csc\theta$$

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Where You Get Complete Knowledge
L.H.S. =
$$\frac{\tan \theta}{1 - \cot \theta} + \frac{\cot \theta}{1 - \tan \theta}$$

= $\frac{\frac{\sin \theta}{1 - \cot \theta} + \frac{\cos \theta}{1 - \tan \theta}$
= $\frac{\frac{\sin \theta}{\cos \theta}}{1 - \frac{\cos \theta}{\sin \theta}} + \frac{\frac{\cos \theta}{\sin \theta}}{\frac{\cos \theta}{\cos \theta}}$
= $\frac{\frac{\sin \theta}{\cos \theta} + \frac{\frac{\cos \theta}{\sin \theta}}{\cos \theta}}{\frac{\cos \theta - \sin \theta}{\cos \theta}}$
= $\frac{\frac{\sin^2 \theta}{\cos \theta (\sin \theta - \cos \theta)} + \frac{\cos^2 \theta}{\sin \theta (\sin \theta - \cos \theta)}$
= $\frac{1}{(\sin \theta - \cos \theta)} \left[\frac{\sin^2 \theta}{\cos \theta} - \frac{\cos^2 \theta}{\sin \theta} \right]$
= $\left(\frac{1}{\sin \theta - \cos \theta} \right) \left[\frac{\sin^3 \theta - \cos^3 \theta}{\sin \theta \cos \theta} \right]$
= $\left(\frac{1}{\sin \theta - \cos \theta} \right) \left[\frac{(\sin \theta - \cos \theta)(\sin^2 \theta + \cos^2 \theta + \sin \theta \cos \theta)}{\sin \theta \cos \theta} \right]$
= $\left(\frac{1}{\sin \theta - \cos \theta} \right)$

 $= \sec\theta \ \csc\theta +$

= R.H.S.

(iv) $\frac{1 + \sec A}{\sec A} = \frac{\sin^2 A}{1 - \cos A}$



Where You Get Complete Knowledge

L.H.S. =
$$\frac{1 + \sec A}{\sec A} = \frac{1 + \frac{1}{\cos A}}{\frac{1}{\cos A}}$$

= $\frac{\frac{\cos A + 1}{\cos A}}{\frac{1}{\cos A}} = (\cos A + 1)$
= $\frac{(1 - \cos A)(1 + \cos A)}{(1 - \cos A)}$
= $\frac{1 - \cos^2 A}{1 - \cos A} = \frac{\sin^2 A}{1 - \cos A}$

= R.H.S

(v) $\frac{\cos A - \sin A + 1}{\cos A + \sin A - 1} = \csc A + \cot A$

Using the identity $\csc^2 A = 1 + \cot^2 A$,

$$L.H.S = \frac{\cos A - \sin A + 1}{\cos A + \sin A - 1}$$



Where You Get Complete Knowledge

$$= \frac{\frac{\cos A}{\sin A} - \frac{\sin A}{\sin A} + \frac{1}{\sin A}}{\frac{\cos A}{\sin A} + \frac{\sin A}{\sin A} + \frac{1}{\sin A}}$$

$$= \frac{\cot A - 1 + \csc A}{\cot A + 1 - \csc A}$$

$$= \frac{\{(\cot A) - (1 - \csc A)\}\{(\cot A) - (1 - \csc A)\}}{\{(\cot A) + (1 - \csc A)\}\{(\cot A) - (1 - \csc A)\}}$$

$$= \frac{(\cot A - 1 + \csc A)^{2}}{(\cot A)^{2} - (1 - \csc A)^{2}}$$

$$= \frac{\cot^{2} A + 1 + \csc^{2} A - 2 \cot A - 2 \csc A + 2 \cot A \csc A}{\cot^{2} A - (1 + \csc^{2} A - 2 \csc A)}$$

$$= \frac{2\csc^{2} A + 2 \cot A \csc A - 2 \cot A - 2 \csc A}{\cot^{2} A - 1 - \csc^{2} A + 2 \csc A}$$

$$= \frac{2\csc A (\csc A + \cot A) - 2(\cot A + \csc A)}{\cot^{2} A - (1 + \csc^{2} A - 1 - 2 \csc A)}$$

$$= \frac{(\csc A + \cot A)(2 \csc A - 2)}{-1 - 1 + 2 \csc A}$$

$$= \operatorname{cosec} A + \operatorname{cot} A$$

= R.H.S

(vi)
$$\sqrt{\frac{1+\sin A}{1-\sin A}} = \sec A + \tan A$$



L.H.S.
$$= \sqrt{\frac{1+\sin A}{1-\sin A}}$$
$$= \sqrt{\frac{(1+\sin A)(1+\sin A)}{(1-\sin A)(1+\sin A)}}$$
$$= \frac{(1+\sin A)}{\sqrt{1-\sin^2 A}} = \frac{1+\sin A}{\sqrt{\cos^2 A}}$$
$$= \frac{1+\sin A}{\cos A} = \sec A + \tan A$$
$$= \text{R.H.S.}$$

(vii)
$$\frac{\sin\theta - 2\sin^3\theta}{2\cos\theta - \cos\theta} = \tan\theta$$

L.H.S. =
$$\frac{\sin \theta - 2\sin^3 \theta}{2\cos^3 \theta - \cos \theta}$$
$$= \frac{\sin \theta (1 - 2\sin^2 \theta)}{\cos \theta (2\cos^2 \theta - 1)}$$
$$= \frac{\sin \theta \times (1 - 2\sin^2 \theta)}{\cos \theta \times \{2(1 - \sin^2 \theta) - 1\}}$$
$$= \frac{\sin \theta \times (1 - 2\sin^2 \theta)}{\cos \theta \times (1 - 2\sin^2 \theta)}$$
$$= \tan \theta = \text{R.H.S}$$

(viii) $(\sin A + \csc A)^2 + (\cos A + \sec A)^2 = 7 + \tan^2 A + \cot^2 A$

L.H.S =
$$(\sin A + \csc A)^2 + (\cos A + \sec A)^2$$

= $\sin^2 A + \csc^2 A + 2\sin A \csc A + \cos^2 A + \sec^2 A + 2\cos A \sec A$
= $(\sin^2 A + \cos^2 A) + (\csc^2 A + \sec^2 A) + 2\sin A \left(\frac{1}{\sin A}\right) + 2\cos A \left(\frac{1}{\cos A}\right)$
= $(1) + (1 + \cot^2 A + 1 + \tan^2 A) + (2) + (2)$
= $7 + \tan^2 A + \cot^2 A$
= R.H.S

(ix)
$$(\operatorname{cosec} A - \sin A)(\operatorname{sec} A - \cos A) = \frac{1}{\tan A + \cot A}$$



Where You Get Complete Knowledge

L.H.S =
$$(\operatorname{cosec} A - \sin A)(\operatorname{sec} A - \cos A)$$

= $\left(\frac{1}{\sin A} - \sin A\right)\left(\frac{1}{\cos A} - \cos A\right)$
= $\left(\frac{1 - \sin^2 A}{\sin A}\right)\left(\frac{1 - \cos^2 A}{\cos A}\right)$
= $\frac{(\cos^2 A)(\sin^2 A)}{\sin A \cos A}$
= $\sin A \cos A$

R.H.S =
$$\frac{1}{\tan A + \cot A}$$

= $\frac{1}{\frac{\sin A}{\cos A} + \frac{\cos A}{\sin A}} = \frac{1}{\frac{\sin^2 A + \cos^2 A}{\sin A \cos A}}$
= $\frac{\sin A \cos A}{\sin^2 A + \cos^2 A} = \sin A \cos A$

Hence, L.H.S = R.H.S

(x)
$$\left(\frac{1+\tan^2 A}{1+\cot^2 A}\right) = \left(\frac{1-\tan A}{1-\cot A}\right)^2 = \tan^2 A$$

$$\frac{1 + \tan^2 A}{1 + \cot^2 A} = \frac{1 + \frac{\sin^2 A}{\cos^2 A}}{1 + \frac{\cos^2 A}{\sin^2 A}} = \frac{\frac{\cos^2 A + \sin^2 A}{\cos^2 A}}{\frac{\sin^2 A + \cos^2 A}{\sin^2 A}}$$
$$= \frac{\frac{1}{\cos^2 A}}{\frac{1}{\sin^2 A}} = \frac{\sin^2 A}{\cos^2 A}$$
$$= \tan^2 A$$



$$\left(\frac{1-\tan A}{1-\cot A}\right)^{2} = \frac{1+\tan^{2} A - 2 \tan A}{1+\cot^{2} A - 2 \cot A}$$
$$= \frac{\sec^{2} A - 2 \cot A}{\cos e^{2} A - 2 \cot A}$$
$$= \frac{\frac{1}{\cos^{2} A} - \frac{2 \sin A}{\cos A}}{\frac{1}{\sin^{2} A} - \frac{2 \cos A}{\sin A}} = \frac{\frac{1-2 \sin A \cos A}{\cos^{2} A}}{\frac{1-2 \sin A \cos A}{\sin^{2} A}}$$
$$= \frac{\sin^{2} A}{\cos^{2} A} = \tan^{2} A$$

 $(1 + \tan \theta + \sec \theta) (1 + \cot \theta - \csc \theta)$

$$= \left(1 + \frac{\sin\theta}{\cos\theta} + \frac{1}{\cos\theta}\right) \left(1 + \frac{\cos\theta}{\sin\theta} - \frac{1}{\sin\theta}\right)$$
$$= \left(\frac{\cos\theta + \sin\theta + 1}{\cos\theta}\right) \left(\frac{\sin\theta + \cos\theta - 1}{\sin\theta}\right)$$
$$= \frac{\left(\sin\theta + \cos\theta\right)^2 - \left(1\right)^2}{\sin\theta\cos\theta}$$
$$= \frac{\sin^2\theta + \cos^2\theta + 2\sin\theta\cos\theta - 1}{\sin\theta\cos\theta}$$
$$= \frac{1 + 2\sin\theta\cos\theta - 1}{\sin\theta\cos\theta}$$
$$= \frac{2\sin\theta\cos\theta}{\sin\theta\cos\theta} = 2$$

Hence, alternative (C) is correct.

(iii) $(\sec A + \tan A) (1 - \sin A)$



Where You Get Complete Knowledge

$$= \left(\frac{1}{\cos A} + \frac{\sin A}{\cos A}\right) (1 - \sin A)$$
$$= \left(\frac{1 + \sin A}{\cos A}\right) (1 - \sin A)$$
$$= \frac{1 - \sin^2 A}{\cos A} = \frac{\cos^2 A}{\cos A}$$

 $= \cos A$

Hence, alternative (D) is correct.

$$\frac{1+\tan^2 A}{1+\cot^2 A} = \frac{1+\frac{\sin^2 A}{\cos^2 A}}{1+\frac{\cos^2 A}{\sin^2 A}}$$

(iv)
$$= \frac{\frac{\cos^2 A+\sin^2 A}{\frac{\sin^2 A+\cos^2 A}{\sin^2 A}} = \frac{\frac{1}{\cos^2 A}}{\frac{1}{\sin^2 A}}$$
$$= \frac{\frac{\sin^2 A}{\cos^2 A}}{\cos^2 A} = \tan^2 A$$

Hence, alternative (D) is correct.

