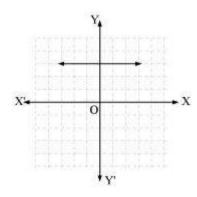
Exercise - 2.1

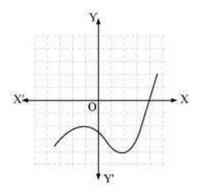
#### Question 1:

The graphs of y = p(x) are given in following figure, for some polynomials p(x). Find the number of zeroes of p(x), in each case.

(i)

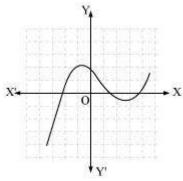


(ii)

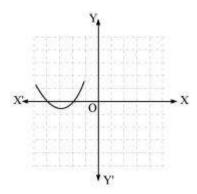


(iii)

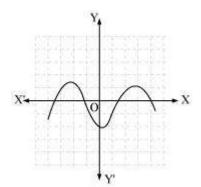




(iv)

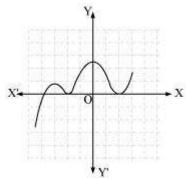


(v)



(v)

#### Where You Get Complete Knowledge



- (i) The number of zeroes is 0 as the graph does not cut the x-axis at any point.
- (ii) The number of zeroes is 1 as the graph intersects the x-axis at only 1 point.
- (iii) The number of zeroes is 3 as the graph intersects the x-axis at 3 points.
- (iv) The number of zeroes is 2 as the graph intersects the x-axis at 2 points.
- (v) The number of zeroes is 4 as the graph intersects the x-axis at 4 points.
- (vi) The number of zeroes is 3 as the graph intersects the x-axis at 3 points.

Exercise - 2.2

#### Question 1:

Find the zeroes of the following quadratic polynomials and verify the relationship between the zeroes and the coefficients.

(i) 
$$x^2 - 2x - 8$$
 (ii)  $4s^2 - 4s + 1$  (iii)  $6x^2 - 3 - 7x$ 

$$(iv) 4u^2 + 8u (v)t^2 - 15 (vi) 3x^2 - x - 4$$

(i) 
$$x^2-2x-8=(x-4)(x+2)$$

The value of  $x^2 - 2x - 8$  is zero when x - 4 = 0 or x + 2 = 0, i.e., when x = 4 or x = -2

Therefore, the zeroes of  $x^2 - 2x - 8$  are 4 and -2.



### Where You Get Complete Knowledge

Sum of zeroes = 
$$4-2=2=\frac{-(-2)}{1}=\frac{-(\text{Coefficient of }x)}{\text{Coefficient of }x^2}$$

Product of zeroes 
$$= 4 \times (-2) = -8 = \frac{(-8)}{1} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

(ii) 
$$4s^2-4s+1=(2s-1)^2$$

The value of  $4s^2 - 4s + 1$  is zero when 2s - 1 = 0, i.e.,  $s = \frac{1}{2}$ 

Therefore, the zeroes of  $4s^2 - 4s + 1$  are  $\frac{1}{2}$  and  $\frac{1}{2}$ .

Sum of zeroes = 
$$\frac{1}{2} + \frac{1}{2} = 1 = \frac{-(-4)}{4} = \frac{-(\text{Coefficient of } s)}{(\text{Coefficient of } s^2)}$$

Product of zeroes 
$$= \frac{1}{2} \times \frac{1}{2} = \frac{1}{4} = \frac{\text{Constant term}}{\text{Coefficient of } s^2}$$

(iii) 
$$6x^2-3-7x=6x^2-7x-3=(3x+1)(2x-3)$$

The value of  $6x^2 - 3 - 7x$  is zero when 3x + 1 = 0 or 2x - 3 = 0, i.e.,  $x = \frac{-1}{3}$  or  $x = \frac{3}{2}$ 

Therefore, the zeroes of  $6x^2 - 3 - 7x$  are  $\frac{-1}{3}$  and  $\frac{3}{2}$ .

Sum of zeroes = 
$$\frac{-1}{3} + \frac{3}{2} = \frac{7}{6} = \frac{-(-7)}{6} = \frac{-(\text{Coefficient of } x)}{\text{Coefficient of } x^2}$$

Product of zeroes = 
$$\frac{-1}{3} \times \frac{3}{2} = \frac{-1}{2} = \frac{-3}{6} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

(iv) 
$$4u^2 + 8u = 4u^2 + 8u + 0$$
  
=  $4u(u+2)$ 

## 3

## **EDUCATION CENTRE**

#### Where You Get Complete Knowledge

The value of  $4u^2 + 8u$  is zero when 4u = 0 or u + 2 = 0, i.e., u = 0 or u = -2

Therefore, the zeroes of  $4u^2 + 8u$  are 0 and -2.

Sum of zeroes = 
$$0 + (-2) = -2 = \frac{-(8)}{4} = \frac{-(\text{Coefficient of } u)}{\text{Coefficient of } u^2}$$

Product of zeroes = 
$$0 \times (-2) = 0 = \frac{0}{4} = \frac{\text{Constant term}}{\text{Coefficient of } u^2}$$

(v) 
$$t^2 - 15$$
  
=  $t^2 - 0.t - 15$   
=  $(t - \sqrt{15})(t + \sqrt{15})$ 

The value of  $t^2 - 15$  is zero when  $t - \sqrt{15} = 0$  or  $t + \sqrt{15} = 0$ , i.e., when  $t = \sqrt{15}$  or  $t = -\sqrt{15}$ 

Therefore, the zeroes of  $t^2 - 15$  are  $\sqrt{15}$  and  $-\sqrt{15}$ .

$$\sqrt{15} + \left(-\sqrt{15}\right) = 0 = \frac{-0}{1} = \frac{-\left(\text{Coefficient of }t\right)}{\left(\text{Coefficient of }t^2\right)}$$
Sum of zeroes =

Product of zeroes = 
$$(\sqrt{15})(-\sqrt{15}) = -15 = \frac{-15}{1} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$$

(vi) 
$$3x^2 - x - 4$$
  
=  $(3x - 4)(x + 1)$ 

The value of  $3x^2 - x - 4$  is zero when 3x - 4 = 0 or x + 1 = 0, i.e., when  $x = \frac{4}{3}$  or x = -1

Therefore, the zeroes of  $3x^2 - x - 4$  are  $\frac{4}{3}$  and -1.

Sum of zeroes = 
$$\frac{4}{3} + (-1) = \frac{1}{3} = \frac{-(-1)}{3} = \frac{-(\text{Coefficient of } x)}{\text{Coefficient of } x^2}$$



#### Where You Get Complete Knowledge

Product of zeroes  $= \frac{4}{3}(-1) = \frac{-4}{3} = \frac{\text{Constant term}}{\text{Coefficient of } x^2}$ 

Question 2:

Find a quadratic polynomial each with the given numbers as the sum and product of its zeroes respectively.

(i) 
$$\frac{1}{4}$$
,-1 (ii)  $\sqrt{2}$ , $\frac{1}{3}$  (iii)  $0$ , $\sqrt{5}$ 

(iv) 
$$_{1,1}$$
 (v)  $-\frac{1}{4}, \frac{1}{4}$  (vi)  $_{4,1}$ 

(i) 
$$\frac{1}{4}$$
,-1

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = \frac{1}{4} = \frac{-b}{a}$$

$$\alpha\beta = -1 = \frac{-4}{4} = \frac{c}{a}$$

If 
$$a = 4$$
, then  $b = -1$ ,  $c = -4$ 

Therefore, the quadratic polynomial is  $4x^2 - x - 4$ .

(ii) 
$$\sqrt{2}, \frac{1}{3}$$

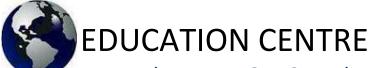
Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = \sqrt{2} = \frac{3\sqrt{2}}{3} = \frac{-b}{a}$$

$$\alpha\beta = \frac{1}{3} = \frac{c}{a}$$

If 
$$a = 3$$
, then  $b = -3\sqrt{2}$ ,  $c = 1$ 

Therefore, the quadratic polynomial is  $3x^2 - 3\sqrt{2}x + 1$ .



(iii) 
$$0, \sqrt{5}$$

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = 0 = \frac{0}{1} = \frac{-b}{a}$$

$$\alpha \times \beta = \sqrt{5} = \frac{\sqrt{5}}{1} = \frac{c}{a}$$

If a = 1, then b = 0,  $c = \sqrt{5}$ 

Therefore, the quadratic polynomial is  $x^2 + \sqrt{5}$ .

(iv) 1, 1

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = 1 = \frac{1}{1} = \frac{-b}{a}$$

$$\alpha \times \beta = 1 = \frac{1}{1} = \frac{c}{a}$$

If 
$$a = 1$$
, then  $b = -1$ ,  $c = 1$ 

Therefore, the quadratic polynomial is  $x^2 - x + 1$ .

$$(v) -\frac{1}{4}, \frac{1}{4}$$

Let the polynomial be  $ax^2 + bx + c$ , and its zeroes be  $\alpha$  and  $\beta$ .

$$\alpha + \beta = \frac{-1}{4} = \frac{-b}{a}$$

$$\alpha \times \beta = \frac{1}{4} = \frac{c}{a}$$

If 
$$a = 4$$
, then  $b = 1$ ,  $c = 1$ 

Therefore, the quadratic polynomial is  $4x^2 + x + 1$ .

Let the polynomial be  $ax^2 + bx + c$ .

$$\alpha + \beta = 4 = \frac{4}{1} = \frac{-b}{a}$$

$$\alpha \times \beta = 1 = \frac{1}{1} = \frac{c}{a}$$

If 
$$a = 1$$
, then  $b = -4$ ,  $c = 1$ 

Therefore, the quadratic polynomial is  $x^2 - 4x + 1$ .

Exercise – 2.3

#### Question 1:

Divide the polynomial p(x) by the polynomial g(x) and find the quotient and remainder in each of the following:

(i) 
$$p(x) = x^3 - 3x^2 + 5x - 3$$
,  $g(x) = x^2 - 2$ 

(ii) 
$$p(x) = x^4 - 3x^2 + 4x + 5$$
,  $g(x) = x^2 + 1 - x$ 

(iii) 
$$p(x) = x^4 - 5x + 6$$
,  $g(x) = 2 - x^2$ 

(i) 
$$p(x) = x^3 - 3x^2 + 5x - 3$$
  
 $q(x) = x^2 - 2$ 

$$\begin{array}{r}
x-3 \\
x^2-2 \overline{)x^3-3x^2+5x-3} \\
x^3 -2x \\
\underline{- + \\
-3x^2+7x-3 \\
-3x^2 +6 \\
\underline{+ - \\
7x-9}
\end{array}$$



#### Where You Get Complete Knowledge

Quotient = x - 3

Remainder = 7x - 9

(ii) 
$$p(x) = x^4 - 3x^2 + 4x + 5 = x^4 + 0.x^3 - 3x^2 + 4x + 5$$
  
 $q(x) = x^2 + 1 - x = x^2 - x + 1$ 

Question 2:

Check whether the first polynomial is a factor of the second polynomial by dividing the second polynomial by the first polynomial:

(i) 
$$t^2 - 3, 2t^4 + 3t^3 - 2t^2 - 9t - 12$$

(ii) 
$$x^2 + 3x + 1, 3x^4 + 5x^3 - 7x^2 + 2x + 2$$

(iii) 
$$x^3 - 3x + 1, x^5 - 4x^3 + x^2 + 3x + 1$$

(i) 
$$t^2-3$$
,  $2t^4+3t^3-2t^2-9t-12$ 

$$t^2 - 3 = t^2 + 0.t - 3$$

$$\begin{array}{r}
2t^2 + 3t + 4 \\
t^2 + 0.t - 3 \overline{)2t^4 + 3t^3 - 2t^2 - 9t - 12} \\
2t^4 + 0.t^3 - 6t^2 \\
\underline{- - + } \\
3t^3 + 4t^2 - 9t - 12 \\
3t^3 + 0.t^2 - 9t \\
\underline{- - + } \\
4t^2 + 0.t - 12 \\
4t^2 + 0.t - 12 \\
\underline{- - + } \\
0
\end{array}$$

Since the remainder is 0,

Hence,  $t^2 - 3$  is a factor of  $2t^4 + 3t^3 - 2t^2 - 9t - 12$ .

#### Where You Get Complete Knowledge

(ii) 
$$x^2 + 3x + 1$$
,  $3x^4 + 5x^3 - 7x^2 + 2x + 2$ 

Since the remainder is 0,

Hence,  $x^2 + 3x + 1$  is a factor of  $3x^4 + 5x^3 - 7x^2 + 2x + 2$ .

(iii) 
$$x^3 - 3x + 1$$
,  $x^5 - 4x^3 + x^2 + 3x + 1$ 

$$\begin{array}{r}
x^{2}-1 \\
x^{3}-3x+1 \overline{\smash)} x^{5}-4x^{3}+x^{2}+3x+1 \\
x^{5}-3x^{3}+x^{2} \\
\underline{-+--} \\
-x^{3} +3x+1 \\
\underline{-x^{3} +3x-1} \\
\underline{+--+} \\
2
\end{array}$$

Since the remainder  $\neq 0$ ,

Hence,  $x^3 - 3x + 1$  is not a factor of  $x^5 - 4x^3 + x^2 + 3x + 1$ .



$$\begin{array}{r}
x^2 + x - 3 \\
x^2 - x + 1 \overline{\smash)} \quad x^4 + 0.x^3 - 3x^2 + 4x + 5 \\
x^4 - x^3 + x^2 \\
\underline{- + -} \\
x^3 - 4x^2 + 4x + 5 \\
x^3 - x^2 + x \\
\underline{- + -} \\
- 3x^2 + 3x + 5 \\
\underline{- 3x^2 + 3x - 3} \\
\underline{+ - +} \\
8
\end{array}$$

Quotient =  $x^2 + x - 3$ 

Remainder = 8

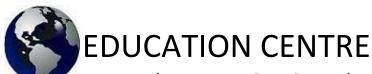
(iii) 
$$p(x) = x^4 - 5x + 6 = x^4 + 0 \cdot x^2 - 5x + 6$$
  
 $q(x) = 2 - x^2 = -x^2 + 2$ 

$$\begin{array}{r}
-x^{2}-2 \\
-x^{2}+2 \overline{)} & x^{4}+0.x^{2}-5x+6 \\
x^{4}-2x^{2} \\
\underline{- + } \\
2x^{2}-5x+6 \\
2x^{2}-4 \\
\underline{- + } \\
-5x+10
\end{array}$$

Quotient =  $-x^2 - 2$ 

Remainder = -5x + 10

Question 3:



Obtain all other zeroes of  $\int_{1}^{3} \sqrt{\frac{1}{3}} = \int_{1}^{3} \sqrt{\frac{1}$ 

$$p(x) = 3x^4 + 6x^3 - 2x^2 - 10x - 5$$

Since the two zeroes are  $\sqrt{\frac{5}{3}}$  and  $-\sqrt{\frac{5}{3}}$ ,

Therefore, we divide the given polynomial by  $x^2 - \frac{5}{3}$ .

$$x^{2} + 0.x - \frac{5}{3} ) \frac{3x^{2} + 6x + 3}{3x^{4} + 6x^{3} - 2x^{2} - 10x - 5}$$

$$3x^{4} + 0x^{3} - 5x^{2}$$

$$- - +$$

$$6x^{3} + 3x^{2} - 10x - 5$$

$$6x^{3} + 0x^{2} - 10x$$

$$- - +$$

$$3x^{2} + 0x - 5$$

$$3x^{2} + 0x - 5$$

$$- - +$$

$$0$$

$$3x^{4} + 6x^{3} - 2x^{2} - 10x - 5 = \left(x^{2} - \frac{5}{3}\right) \left(3x^{2} + 6x + 3\right)$$

$$= 3\left(x^{2} - \frac{5}{3}\right) \left(x^{2} + 2x + 1\right)$$

We factorize  $x^2 + 2x + 1$ 



#### Where You Get Complete Knowledge

$$=(x+1)^2$$

Therefore, its zero is given by x + 1 = 0

$$\chi = -1$$

As it has the term  $(x+1)^2$ , therefore, there will be 2 zeroes at x=-1.

Hence, the zeroes of the given polynomial are  $\sqrt{\frac{5}{3}}$ ,  $-\sqrt{\frac{5}{3}}$ , -1 and -1.

Question 4:

On dividing  $x^3 - 3x^2 + x + 2$  by a polynomial g(x), the quotient and remainder were x - 2 and -2x + 4, respectively. Find g(x).

$$p(x) = x^3 - 3x^2 + x + 2$$
 (Dividend)

$$g(x) = ?$$
 (Divisor)

Quotient = 
$$(x - 2)$$

Remainder = 
$$(-2x + 4)$$

 $Dividend = Divisor \times Quotient + Remainder$ 

$$x^3 - 3x^2 + x + 2 = g(x) \times (x - 2) + (-2x + 4)$$

$$x^3 - 3x^2 + x + 2 + 2x - 4 = g(x)(x-2)$$

$$x^3 - 3x^2 + 3x - 2 = g(x)(x-2)$$

g(x) is the quotient when we divide  $(x^3-3x^2+3x-2)$  by (x-2)



#### Where You Get Complete Knowledge

$$\begin{array}{r}
x^{2} - x + 1 \\
x - 2) \overline{)x^{3} - 3x^{2} + 3x - 2} \\
x^{3} - 2x^{2} \\
\underline{- + } \\
-x^{2} + 3x - 2 \\
-x^{2} + 2x \\
\underline{+ - } \\
x - 2 \\
x - 2 \\
\underline{- + } \\
0
\end{array}$$

$$\therefore g(x) = (x^2 - x + 1)$$

Question 5:

Give examples of polynomial p(x), g(x), q(x) and r(x), which satisfy the division algorithm and

(i) 
$$\deg p(x) = \deg q(x)$$

(ii) 
$$\deg q(x) = \deg r(x)$$

(iii) 
$$\deg r(x) = 0$$

According to the division algorithm, if p(x) and g(x) are two polynomials with

 $g(x) \neq 0$ , then we can find polynomials q(x) and r(x) such that

$$p(x) = g(x) \times q(x) + r(x),$$

where r(x) = 0 or degree of r(x) <degree of g(x)

Degree of a polynomial is the highest power of the variable in the polynomial.

(i) 
$$\deg p(x) = \deg q(x)$$



Degree of quotient will be equal to degree of dividend when divisor is constant ( i.e., when any polynomial is divided by a constant).

Let us assume the division of  $6x^2 + 2x + 2$  by 2.

Here, 
$$p(x) = 6x^2 + 2x + 2$$

$$g(x) = 2$$

$$q(x) = 3x^2 + x + 1$$
 and  $r(x) = 0$ 

Degree of p(x) and q(x) is the same i.e., 2.

Checking for division algorithm,

$$p(x) = g(x) \times q(x) + r(x)$$

$$6x^2 + 2x + 2 = 2(3x^2 + x + 1)$$

$$= 6x^2 + 2x + 2$$

Thus, the division algorithm is satisfied.

(ii) 
$$\deg q(x) = \deg r(x)$$

Let us assume the division of  $x^3 + x$  by  $x^2$ ,

Here, 
$$p(x) = x^3 + x$$

$$g(x) = x^2$$

$$q(x) = x$$
 and  $r(x) = x$ 

Clearly, the degree of q(x) and r(x) is the same i.e., 1.

Checking for division algorithm,

$$p(x) = g(x) \times q(x) + r(x)$$



$$\chi^3 + \chi = (\chi^2) \times \chi + \chi$$

$$\chi^3 + \chi = \chi^3 + \chi$$

Thus, the division algorithm is satisfied.

(iii)deg 
$$r(x) = 0$$

Degree of remainder will be 0 when remainder comes to a constant.

Let us assume the division of  $x^3 + 1$ by  $x^2$ .

Here, 
$$p(x) = x^3 + 1$$

$$g(x) = x^2$$

$$q(x) = x$$
 and  $r(x) = 1$ 

Clearly, the degree of r(x) is 0.

Checking for division algorithm,

$$p(x) = g(x) \times q(x) + r(x)$$

$$x^3 + 1 = (x^2) \times x + 1$$

$$x^3 + 1 = x^3 + 1$$

Thus, the division algorithm is satisfied.

Exercise – 2.4

#### Question 1:

Verify that the numbers given alongside of the cubic polynomials below are their zeroes. Also verify the relationship between the zeroes and the coefficients in each case:

# 3

## **EDUCATION CENTRE**

#### Where You Get Complete Knowledge

(i) 
$$2x^3 + x^2 - 5x + 2$$
;  $\frac{1}{2}$ , 1, -2

(ii) 
$$x^3 - 4x^2 + 5x - 2$$
; 2,1,1

(i) 
$$p(x) = 2x^3 + x^2 - 5x + 2$$
.

Zeroes for this polynomial are  $\frac{1}{2}$ , 1, -2

$$p\left(\frac{1}{2}\right) = 2\left(\frac{1}{2}\right)^3 + \left(\frac{1}{2}\right)^2 - 5\left(\frac{1}{2}\right) + 2$$
$$= \frac{1}{4} + \frac{1}{4} - \frac{5}{2} + 2$$
$$= 0$$

$$p(1) = 2 \times 1^3 + 1^2 - 5 \times 1 + 2$$
  
= 0

$$p(-2) = 2(-2)^3 + (-2)^2 - 5(-2) + 2$$
$$= -16 + 4 + 10 + 2 = 0$$

Therefore,  $\frac{1}{2}$ , 1, and -2 are the zeroes of the given polynomial.

Comparing the given polynomial with  $ax^3 + bx^2 + cx + d$ , we obtain a = 2, b = 1, c = -5, d = 2

We can take  $\alpha = \frac{1}{2}$ ,  $\beta = 1$ ,  $\gamma = -2$ 

$$\alpha + \beta + \gamma = \frac{1}{2} + 1 + (-2) = -\frac{1}{2} = \frac{-b}{a}$$

$$\alpha\beta + \beta\gamma + \alpha\gamma = \frac{1}{2} \times 1 + 1(-2) + \frac{1}{2}(-2) = \frac{-5}{2} = \frac{c}{a}$$

$$\alpha\beta\gamma = \frac{1}{2} \times 1 \times \left(-2\right) = \frac{-1}{1} = \frac{-(2)}{2} = \frac{-d}{a}$$

Therefore, the relationship between the zeroes and the coefficients is verified.

(ii) 
$$p(x) = x^3 - 4x^2 + 5x - 2$$



#### Where You Get Complete Knowledge

Zeroes for this polynomial are 2, 1, 1.

$$p(2) = 2^3 - 4(2^2) + 5(2) - 2$$
  
= 8 - 16 + 10 - 2 = 0

$$p(1) = 1^3 - 4(1)^2 + 5(1) - 2$$
$$= 1 - 4 + 5 - 2 = 0$$

Therefore, 2, 1, 1 are the zeroes of the given polynomial.

Comparing the given polynomial with  $ax^3 + bx^2 + cx + d$ , we obtain a = 1, b = -4, c = 5, d = -2.

Verification of the relationship between zeroes and coefficient of the given polynomial

Sum of zeroes = 
$$2+1+1=4=\frac{-(-4)}{1}=\frac{-b}{a}$$

Multiplication of zeroes taking two at a time =  $(2)(1) + (1)(1) + (2)(1) = 2 + 1 + 2 = 5 = \frac{(5)}{1} = \frac{c}{a}$ 

Multiplication of zeroes = 
$$2 \times 1 \times 1 = 2$$
 =  $\frac{-(-2)}{1} = \frac{-d}{a}$ 

Hence, the relationship between the zeroes and the coefficients is verified.

Question 2:

Find a cubic polynomial with the sum, sum of the product of its zeroes taken two at a time, and the product of its zeroes as 2, -7, -14 respectively.

Let the polynomial be  $ax^3 + bx^2 + cx + d$  and the zeroes be  $\alpha, \beta$ , and  $\gamma$ .

It is given that



#### Where You Get Complete Knowledge

$$\alpha + \beta + \gamma = \frac{2}{1} = \frac{-b}{a}$$

$$\alpha\beta + \beta\gamma + \alpha\gamma = \frac{-7}{1} = \frac{c}{a}$$

$$\alpha\beta\gamma = \frac{-14}{1} = \frac{-d}{a}$$

If 
$$a = 1$$
, then  $b = -2$ ,  $c = -7$ ,  $d = 14$ 

Hence, the polynomial is  $x^3 - 2x^2 - 7x + 14$ .

Question 3:

If the zeroes of polynomial  $x^3 - 3x^2 + x + 1$  are a - b, a, a + b, find a and b.

$$p(x) = x^3 - 3x^2 + x + 1$$

Zeroes are a - b, a + a + b

Comparing the given polynomial with  $px^3 + qx^2 + rx + t$ , we obtain

$$p = 1, q = -3, r = 1, t = 1$$

Sum of zeroes = a - b + a + a + b

$$\frac{-q}{p} = 3a$$

$$\frac{-(-3)}{1} = 3a$$

$$3 = 3a$$

$$a = 1$$

The zeroes are 1-b, 1, 1+b.



#### Where You Get Complete Knowledge

Multiplication of zeroes = 1(1-b)(1+b)

$$\frac{-t}{p} = 1 - b^2$$

$$\frac{-1}{1} = 1 - b^2$$

$$1-b^2 = -1$$

$$1+1=b^2$$

$$b = \pm \sqrt{2}$$

Hence, a = 1 and  $b = \sqrt{2}$  or  $-\sqrt{2}$ .

Question 4:

IIt two zeroes of the polynomial  $x^4 - 6x^3 - 26x^2 + 138x - 35$  are  $2 \pm \sqrt{3}$ , find other zeroes.

Given that  $2 + \sqrt{3}$  and  $2 - \sqrt{3}$  are zeroes of the given polynomial.

Therefore, 
$$(x-2-\sqrt{3})(x-2+\sqrt{3}) = x^2 + 4 - 4x - 3$$

 $= x^2 - 4x + 1$  is a factor of the given polynomial

For finding the remaining zeroes of the given polynomial, we will find the quotient by dividing  $x^4 - 6x^3 - 26x^2 + 138x - 35$  by  $x^2 - 4x + 1$ .



#### Where You Get Complete Knowledge

$$\begin{array}{r}
x^2 - 2x - 35 \\
x^2 - 4x + 1 \overline{)} x^4 - 6x^3 - 26x^2 + 138x - 35 \\
x^4 - 4x^3 + x^2 \\
- + - \\
-2x^3 - 27x^2 + 138x - 35 \\
-2x^3 + 8x^2 - 2x \\
+ - + \\
-35x^2 + 140x - 35 \\
-35x^2 + 140x - 35 \\
+ - + \\
0
\end{array}$$

Clearly, 
$$x^4 - 6x^3 - 26x^2 + 138x - 35 = (x^2 - 4x + 1)(x^2 - 2x - 35)$$

It can be observed that  $(x^2-2x-35)$  is also a factor of the given polynomial.

And 
$$(x^2-2x-35) = (x-7)(x+5)$$

Therefore, the value of the polynomial is also zero when x-7=0 or x+5=0

Or 
$$x = 7$$
 or  $-5$ 

Hence, 7 and -5 are also zeroes of this polynomial.

Question 5:

If the polynomial  $x^4 - 6x^3 + 16x^2 - 25x + 10$  is divided by another polynomial  $x^2 - 2x + k$ , the remainder comes out to be x + a, find k and a.

By division algorithm,

 $Dividend = Divisor \times Quotient + Remainder$ 

 $Dividend - Remainder = Divisor \times Quotient$ 

#### Where You Get Complete Knowledge

 $x^4 - 6x^3 + 16x^2 - 25x + 10 - x - a = x^4 - 6x^3 + 16x^2 - 26x + 10 - a$  will be perfectly divisible by  $x^2 - 2x + k$ .

Let us divide  $x^4 - 6x^3 + 16x^2 - 26x + 10 - a$  by  $x^2 - 2x + k$ 

It can be observed that  $(-10+2k)x+(10-a-8k+k^2)$  will be 0.

Therefore, 
$$(-10+2k) = 0$$
 and  $(10-a-8k+k^2) = 0$ 

For 
$$(-10+2k) = 0$$
,

$$2 k = 10$$

And thus, k = 5

For 
$$(10-a-8k+k^2)=0$$

$$10 - a - 8 \times 5 + 25 = 0$$

$$10 - a - 40 + 25 = 0$$

$$-5 - a = 0$$

Therefore, a = -5

Hence, k = 5 and a = -5